Development of microbial-enzyme-mediated decomposition model parameters through steady-state and dynamic analyses

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Abstract. We developed a microbial-enzyme-mediated decomposition (MEND) model, based on the Michaelis-Menten kinetics, that describes the dynamics of physically defined pools of soil organic matter (SOC). These include particulate, mineral-associated, dissolved organic matter (POC, MOC, and DOC, respectively), microbial biomass, and associated exoenzymes. The ranges and/or distributions of parameters were determined by both analytical steady-state and dynamic analyses with SOC data from the literature. We used an improved multi-objective parameter sensitivity analysis (MOPSA) to identify the most important parameters for the full model: maintenance of microbial biomass, turnover and synthesis of enzymes, and carbon use efficiency (CUE). The model predicted that an increase of 2°C (baseline temperature 12°C) caused the pools of POC-cellulose, MOC, and total SOC to increase with dynamic CUE and decrease with constant CUE, as indicated by the 50% confidence intervals. Regardless of dynamic or constant CUE, the changes in pool size of POC, MOC, and total SOC varied from −8% to 8% under +2°C. The scenario analysis using a single parameter set indicates that higher temperature with dynamic CUE might result in greater net increases in both POC-cellulose and MOC pools. Different dynamics of various SOC pools reflected the catalytic functions of specific enzymes targeting specific substrates and the interactions between microbes, enzymes, and SOC. With the feasible parameter values estimated in this study, models incorporating fundamental principles of microbial-enzyme dynamics can lead to simulation results qualitatively different from traditional models with fast/slow/passive pools.

Key words: decomposition; microbial biomass; multi-objective parameter sensitivity analysis (MOPSA); parameterization; soil enzymes.

INTRODUCTION

Recent developments in modeling of soil organic carbon (SOC) decomposition have explicitly taken into account the role of microbes as decomposers (Schimel and Wintraub 2003, Moorhead and Sinsabaugh 2006, Lawrence et al. 2009, Allison et al. 2010). Particularly, these models separate extracellular enzymes from the microbial biomass pool and directly couple the kinetics of enzymes to SOC turnover. Schimel and Wintraub (2003) incorporated an enzyme pool into a first-order or a reverse Michaelis-Menten (RM-M-SW) kinetics for SOC decomposition. Moorhead and Sinsabaugh (2006) divided the microbial community for litter decomposition into three guilds: opportunists, decomposers, and miners, which are responsible for degradation of soluble substrates, holocellulosates, and lignins, respectively. This guild-based model considered the lignocellulose index (LCI) as a key factor controlling the interactions between lignin and cellulose. The RM-M-SW was used by Lawrence et al. (2009) in an enzyme-catalyzed model including both sorption and desorption processes. Allison et al. (2010) developed a microbial-enzyme model with the Michaelis-Menten (M-M) kinetics to simulate the responses of SOC to an increase of 5°C from 20°C using a single SOC pool.

These efforts were effective attempts to add microbial-enzyme mechanisms to traditional SOC decomposition models. However, several important issues remain to be addressed and further studied:

1) Representation of carbon pools. A single SOC pool or traditional fast/slow/passive pools are often used in SOC decomposition models. Traditional fast/slow/passive pools based on decay rates are empirical and difficult to relate to measurements (Schmidt et al. 2011). Although physically defined SOC fractions have been employed to study SOC dynamics (Six et al. 2001), they have not been considered in SOC decomposition models. Generally, the organic material in the mineral soil can be separated into particulate organic matter (POC) and mineral-associated organic matter (MOC; Schlesinger and Lichter 2001). POC, derived from plants, is defined as the organic matter carbon associated with sand-sized particles (e.g., particle size >53 μm), while MOC refers to the fraction with particle size...
<53 μm (Aoyama et al. 1999, Mrabet et al. 2001, Schlesinger and Lichter 2001, Mendham et al. 2004). POC corresponds to the available SOC in Schimel and Weintraub (2003), and MOC is the physiochemically protected SOC in Conant et al. (2011). Turnover of POC can be orders of magnitude faster than those for MOC (Conant et al. 2011).

2) Representation of enzyme kinetics in models. Since SOC is largely decomposed as a result of exoenzymes produced by microorganisms, explicit representation of enzyme kinetics is an important advance in the process description of SOC dynamics. Several models used the RM-M-SW equation to simulate SOC decomposition, which relies on the concentration of enzymes rather than the concentration of substrates. Unlike the original M-M equation derived from a solid theoretical basis for a simple enzyme and a single substrate (Park and Agmon 2008), the RM-M-SW is functionally analogous to the Langmuir adsorption equation (Schimel and Weintraub 2003). However, almost no estimates of the half-saturation constant for enzyme pools in the RM-M-SW have been reported (Moorhead and Sinsabaugh 2006, Lawrence et al. 2009). Thus it is more difficult to parameterize a RM-M-SW model than a M-M model. Even for the M-M kinetics, very few estimates of the maximum specific reaction rate and the half-saturation constant for substrates have been presented outside of the aquatic literature (Moorhead and Sinsabaugh 2006).

3) Adsorption and desorption of dissolved organic carbon (DOC). The transformation of DOC is one of the rate-limiting steps in decomposition and respiration (Conant et al. 2011). In addition, DOC availability, especially in deeper soil, is controlled by sorption processes (Michalzik et al. 2003). Equilibrium sorption models (e.g., Langmuir isotherm) have been widely used to describe the adsorption/desorption processes (Kaiser and Guggenberger 2000, Hinz 2001, Kaiser et al. 2001, Neff and Asner 2001, Jardine et al. 2006, Kleber et al. 2007, Vandenbruwane et al. 2007, Mehdì et al. 2009). However, equilibrium models are not enough to account for the role of mineral-organic interactions in stabilizing SOC, since they assume that exchange between the adsorbed and dissolved phases equilibrates rapidly (Yurova et al. 2008). Actually, a 24-hour duration has been widely used in the laboratory sorption experiments (Lilienfìein et al. 2004, Kothawala et al. 2008). In addition, the utilization of equilibrium models means that only net adsorption occurs even at low DOC concentration and would result in continuous augmentation of adsorbed C, which is inconsistent with the existence of a maximum sorption capacity denoted by \( Q_{\text{max}} \) (Kothawala et al. 2008, Mayes et al. 2012). Only one model includes both adsorption and desorption (Lawrence et al. 2009), where the adsorption and desorption depend on DOC concentration and slow pool size, respectively. However, the slow pool size in their model was far greater than \( Q_{\text{max}} \). Additionally, the adsorption only depends on the concentration of DOC in their model (Neff and Asner 2001) and disregards the amount of mineral surface available for adsorption (Sohn and Kim 2005).

4) Microbial growth and maintenance. Both growth and maintenance respiration were included in two models, with maintenance respiration proportional to microbial biomass carbon (MBC; Schimel and Weintraub 2003, Lawrence et al. 2009). Wang and Post (2012) conducted a theoretical reassessment of microbial maintenance and proposed a new model scheme to quantify growth respiration rate, maintenance respiration rate, enzyme production rate, plus microbial mortality rate, where the maintenance respiration was considered to depend on both DOC and MBC. This representation of microbial maintenance respiration is adopted in MEND developed here.

5) Model parameterization. One reason that various mechanistic processes have not been integrated into current SOC models is data unavailability (Schmidt et al. 2011). In the previous models, many parameter values were simply assumed by the researchers. Particularly, very few estimates for the kinetic parameters in the M-M equation and the adsorption/desorption rates have been documented for use in models. In addition, model development also requires determination of the relative importance of each parameter for model performance in order to evaluate the adequacy of the model parameter estimates (Wang et al. 2009, Schmidt et al. 2011).

In this study, we developed a microbial-enzyme-mediated SOC decomposition model by considering the aforementioned issues and estimated parameter values through both analytical steady-state and dynamic analyses. Using the estimated parameter ranges/distributions, we implemented a multi-objective parameter sensitivity analysis (MOPSA) to identify important parameters and investigated the effects of temperature on SOC dynamics.

**METHODS**

**Model description**

Carbon pools and fluxes in the proposed microbial-enzyme-mediated decomposition (MEND) model are shown in Fig. 1. Six carbon pools are considered in MEND: (1) particulate organic carbon (POC, represented by the variable \( P \) in model equations, see Table 1), (2) mineral-associated organic carbon (MOC, \( M \)), (3) active layer of MOC interacting with dissolved organic carbon through adsorption and desorption (\( Q \)), (4) dissolved organic carbon (DOC, \( D \)), (5) microbial biomass carbon (MBC, \( B \)), and (6) extracellular enzymes (EP and EM). The component fluxes are (1) DOC uptake by microbes (denoted by the flux \( F_1 \)), (2) POC decomposition \( (F_2) \), (3) MOC decomposition \( (F_3) \), (4, 5) microbial growth respiration \( (F_4) \) and maintenance respiration \( (F_5) \), (6, 7) adsorption \( (F_6) \) and desorption \( (F_7) \), (8) microbial mortality \( (F_8) \), (9) enzyme
production \((F_9)\), and \((10)\) enzyme turnover \((F_{10})\). Model equations for each compartment are listed as follows:

\[
dP \frac{dt}{dt} = IP + \left(1 - gD\right)F_8 - F_2 \tag{1}
\]

\[
dM \frac{dt}{dt} = \left(1 - fD\right)F_2 - F_3 \tag{2}
\]

\[
dQ \frac{dt}{dt} = F_6 - F_7 \tag{3}
\]

\[
dB \frac{dt}{dt} = F_1 - \left(F_4 + F_5\right) - F_8 - (F_{9,EP} + F_{9,EM}) \tag{4}
\]

\[
dD \frac{dt}{dt} = I_D + fD \cdot F_2 + gD \cdot F_8 + F_3 + \left(F_{10,EP} + F_{10,EM}\right) - \left(F_6 - F_7\right) \tag{5}
\]

\[
dEP \frac{dt}{dt} = F_{9,EP} - F_{10,EP} \tag{6}
\]

\[
dEM \frac{dt}{dt} = F_{9,EM} - F_{10,EM} \tag{7}
\]

\[
d \frac{dt}{dt} = \left(P + M + Q + B + D + EP + EM\right)
\]

\[
= IP + I_D - \left(F_4 + F_5\right) \tag{8}
\]

where \(F_i (i = 1, 2, \ldots, 10)\) denotes the component C fluxes,

\[
F_1 = \frac{1}{E_C} (V_D + m_R) \frac{D \times B}{K_D + D} \tag{9}
\]

\[
F_2 = \frac{V_P \times EP \times P}{K_P + P} \tag{10}
\]

\[
F_3 = \frac{V_M \times EM \times M}{K_M + M} \tag{11}
\]

\[
F_4 = \left(1 - \frac{1}{E_C}\right) \frac{V_D \times B \times D}{K_D + D} \tag{12}
\]

\[
F_5 = \left(1 - \frac{1}{E_C}\right) \frac{m_R \times B \times D}{K_D + D} \tag{13}
\]
where the state variables (C pools, i.e., EP, and EM) and model parameters/inputs (e.g., $V_P$, $K_P$, $V_M$, $K_M$, $K_D$, $V_D$, $m_R$, $g_D$, $f_D$, $K_{ads}$, $K_{des}$, $m_P$, $E_C$, $Q_{max}$, $Q_{D}$, binding affinity [$K_{BA}$]) and external inputs ($I = I_P$ and $I_D$) were summarized through Table 1 and Table 2, respectively. Eq. 8 expresses the overall mass balance of the full system.

The POC and DOC pools receive external inputs such as litter decomposition, plant roots, and root exudates (Kuzyakov and Domanski 2000). The decomposition processes of POC and MOC are mediated by responsible enzymes (EP and EM), respectively. A fraction ($f_D$) of decomposed POC enters the DOC pool and the rest ($1 - f_D$) goes to MOC. Decomposed MOC becomes another source for DOC. A pool ($Q$) is differentiated from MOC and defined as the adsorbed phase of DOC interacting with MOC through adsorption and desorption. The potential size of the $Q$ pool is quantified by the maximum adsorption capacity ($Q_{max}$) (Kothawala et al. 2008). We assumed that the mutual conversion between MOC and Q could be neglected. The adsorption and desorption of DOC are simultaneously considered as dynamic processes in the model. The adsorption is controlled by DOC concentration and mineral surface coverage, and the desorption is presumed to only depend on surface coverage (Rudzinski and Panczyk 2000, Sohn and Kim 2005). Relative saturation of the $Q$ pool ($Q/Q_{max}$, ratio of actual adsorbed C content to $Q_{max}$) is defined to represent the fraction of the mineral surface area occupied.

Both growth and maintenance respiratory rates (Pirt 1965, van Iersel and Seymour 2000, Jin and Bethke 2003, van Bodegom 2007) are included in the model. The uptake of DOC by MBC, and the growth, maintenance, and turnover of MBC, follow the model scheme described by Wang and Post (2012). Small portions ($p_{EP}$ and $p_{EM}$) of the physiological maintenance of MBC (quantified by the factor $m_R$) are allocated to enzyme production, and the turnover of MBC enters DOC with a fraction of $g_D$ and POC with the rest of the fraction of ($1 - g_D$).

In this paper, DOC is considered as potential DOC, passing a filter pore size of 0.4–0.6 μm (Novak et al. 1992, Kalbitz et al. 2000, Chantigny 2003), that contains organic carbon from the decomposition of POC and MOC, the desorption of C from mineral surfaces, enzymes, and the death of MBC. It is similar to the concept of “available DOC” postulated by Schimel and Weintraub (2003) and “soluble organic carbon” used by Qualts (2000). Therefore, the DOC used in our model includes DOC present in soil solution and potentially soluble organic carbon, but in solid state.

**Model parameterization**

Data for SOC, DOC, and MBC, and related climate, soil, and land use conditions were collected from 985 observations in 177 publications (see full data in the Supplement). Generally, the depth of these soil samples ranged from 0.1 to 0.5 m with an average depth of 0.25 m. In addition, values for some parameters (e.g., $K_D$, $m_R$, $E_C$, $Q_{max}$, binding affinity [$K_{BA}$]) and external inputs ($I = I_P + I_D$) were also summarized through literature research (Wang et al. 2012b). Based on these

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**Table 2. Model parameters and inputs.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V_P$</td>
<td>maximum specific decomposition rate for $P$ by EP</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$K_P$</td>
<td>half-saturation constant for decomposition of $P$</td>
<td>mg C/g soil</td>
</tr>
<tr>
<td>$V_M$</td>
<td>maximum specific decomposition rate for $M$ by EM</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$K_M$</td>
<td>half-saturation constant for decomposition of $M$</td>
<td>mg C/g soil</td>
</tr>
<tr>
<td>$V_D$</td>
<td>maximum specific uptake rate of $D$ for growth of $B$</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$K_D$</td>
<td>half-saturation constant of uptake of $D$ for growth of $B$</td>
<td>mg C/g soil</td>
</tr>
<tr>
<td>$m_R$</td>
<td>specific maintenance factor or rate</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$E_C$</td>
<td>carbon use efficiency</td>
<td></td>
</tr>
<tr>
<td>$f_D$</td>
<td>fraction of decomposed $P$ allocated to $D$</td>
<td></td>
</tr>
<tr>
<td>$g_D$</td>
<td>fraction of dead $B$ allocated to $D$</td>
<td></td>
</tr>
<tr>
<td>$p_{EP}$</td>
<td>fraction of $m_R$ for production of EP</td>
<td></td>
</tr>
<tr>
<td>$p_{EM}$</td>
<td>fraction of $m_R$ for production of EM</td>
<td></td>
</tr>
<tr>
<td>$r_{EP}$</td>
<td>turnover rate of EP</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$r_{EM}$</td>
<td>turnover rate of EM</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$Q_{max}$</td>
<td>maximum DOC sorption capacity</td>
<td>mg C/g soil</td>
</tr>
<tr>
<td>$K_{ads}$</td>
<td>specific adsorption rate</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$K_{des}$</td>
<td>adsorption rate</td>
<td>mg C·mg C$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$K_{BA}$</td>
<td>binding affinity</td>
<td>(mg C/g soil)$^{-1}$</td>
</tr>
<tr>
<td>$I_P$</td>
<td>input rate of $P$</td>
<td>mg C/g soil$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$I_D$</td>
<td>input rate of $D$</td>
<td>mg C/g soil$^{-1}$·h$^{-1}$</td>
</tr>
<tr>
<td>$h_D$</td>
<td>ratio of $I_D$ to $I_P$</td>
<td></td>
</tr>
</tbody>
</table>
data and the steady-state solutions, values or ranges for the other model parameters could be estimated. From the analysis of Wang and Post (2012), the values of specific maintenance rate, maintenance coefficient, and turnover rate of MBC were combined to quantify the specific maintenance factor (mK). Literature values of K_{BA} are expressed in units of (mg C/g soil)^{-1} because it is usually derived from sorption experiments using soil solutions. We converted K_{BA} to values in units of (mg C/L solution)^{-1} by presuming that the dimensionless quantities, D_{eq}K_{BA} (D_{eq} is the equilibrium concentration of DOC), are equivalent under different unit systems.

Statistical analysis of literature data was conducted using R software (R Development Core Team 2011). The Kolmogorov-Smirnov goodness-of-fit (KS) test was adopted for the normality test (software available online).2 The significance of difference between categorical data was tested by the non-parametric Kruskal-Wallis (KW) test (see footnote 2; Ott and Longnecker 2010). Both KS and KW tests were conducted at a significance level of 0.05.

**Multi-objective parameter sensitivity analysis**

The parametric sensitivity analysis is important for model parameterization (Wang and Chen 2012, Wang et al. 2012a). Based on the estimated parameter ranges, we could identify the critical parameters for the dynamics of each pool through an improved multi-objective parameter sensitivity analysis (MOPSA). The original MOPSA in Wang and Chen (2012) was developed based on the multi-parameter sensitivity analysis (MPSA) algorithm, which is a global sensitivity analysis method (Rodriguez-Fernandez et al. 2012). The consideration of multiple objectives is essential in models with many processes and state variables (Wang and Xia 2010). We used this improved MOPSA approach to increase our ability to quantitatively interpret the results over previous MPSA in Wang and Chen (2012). The improved MOPSA consists of the following steps:

1) Select the parameters to be evaluated and generate parameter sets in terms of their distributions and ranges based on the parameterization process described in the previous section.

2) Run the model with these parameter sets and compute the objective function values (OBFs) in terms of a specific response variable. The OBFs are defined as the sum of squared errors between observed and simulated time-series data. In particular, observed values achieve the OBF using the medians of parameters.

3) Identify whether the parameter sets are acceptable or unacceptable by comparing the OBFs to a given criterion, e.g., the 50% divisions of the sorted OBFs (Choi et al. 1998). The OBF less than the criterion is classified as acceptable, otherwise it is classified as unacceptable.

4) For the jth parameter, if it follows a log-transformed distribution (e.g., log-normal or log-uniform has been used in step 1), let Xi = \{x_{ij}, j = 1, 2, \ldots, 2n\} be the logarithmic parameter values; otherwise, let Xi be the original values. Define x_{imin} = min\{Xi\} and x_{imax} = max\{Xi\}, and the normalized Xi, denoted by Xni = \{x_{ni,j}, j = 1, 2, \ldots, 2n\}, is defined as

\[
X_{ni,j} = \frac{x_{ij} - x_{imin}}{x_{imax} - x_{imin}} \in [0, 1].
\]  

5) Let \(X_n^A = \{x_{ni,j}, j = 1, 2, \ldots, n\}\) and \(X_n^U = \{x_{ni,j}, j = 1, 2, \ldots, n\}\) be the sorted (in ascending order) subsets of acceptable (A) and unacceptable (U)Xni, respectively. Plot the cumulative probability distribution (CPD) curves for the acceptable and unacceptable subsets. Compute the average “discrepancy” between the two CPD curves as the sensitivity index (SI):

\[
SI_i = \frac{1}{n} \sum_{j=1}^{n} \left| X_{ni,j}^A - X_{ni,j}^U \right|
\]

where SI_i is the sensitivity index of the ith parameter for the kth response variable.

6) Evaluate the sensitivity of each parameter by the sensitivity plots and the SI values. The sensitivity plot qualitatively shows the discrepancy between the two CPD curves. In addition, the SI value quantitatively describes the relative sensitivity between parameters. A large difference means that the response variable is highly sensitive to the changes in that parameter. Similarly, a higher SI value implies a higher sensitivity of the parameter.

7) The above analysis is conducted for a single objective (i.e., a single response variable). The overall parameter sensitivity index of a model with multiple response variables can be estimated as

\[
SI_i = \frac{1}{m} \sum_{k=1}^{m} SI_i^k
\]

where SI_i denotes the overall sensitivity index for the ith parameter in terms of m response variables.

Log-normalization is required for those parameters with log-transformed distributions in step 4 to make the sensitivity plots and the SI values comparable among parameters. The sensitivity index used here is a relative concept. The SI values can be used to compare the sensitivities between different parameters pertaining to a specific objective function or an integrated function of multi-objective. A parameter with higher SI value is more sensitive (or important) than another parameter with lower SI value.

**SOC responses to warming: model application**

The SOC dynamics is influenced by environmental factors, especially temperature (Davidson and Janssens...
Table 3. Activation energies (Ea) for selected parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Activation energy (kJ/mol)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vₚ₇, lignin</td>
<td>53 ± 17</td>
<td>Wang et al. (2012b)</td>
</tr>
<tr>
<td>Vₚ₇, cellulose</td>
<td>37 ± 15</td>
<td>Wang et al. (2012b)</td>
</tr>
<tr>
<td>Vₚ₆, V₉₇</td>
<td>47</td>
<td>Allison et al. (2010)</td>
</tr>
<tr>
<td>Kₚ₆, K₉₇, Kₛ₄</td>
<td>30</td>
<td>Davidson et al. (2006)</td>
</tr>
<tr>
<td>mₛ₄</td>
<td>20</td>
<td>van Iersel and Seymour (2002)</td>
</tr>
<tr>
<td>Kₙₛ₄, Kₙ₉₇</td>
<td>5</td>
<td>Elshafei et al. (2009)</td>
</tr>
<tr>
<td>Kₙₙₛ₄</td>
<td>20</td>
<td>Kaiser et al. (2001)</td>
</tr>
</tbody>
</table>

Note: Activation energy values for Vₚ₇ are means ± SD.

2006). However, the impacts of warming on SOC dynamics are uncertain (Conant et al. 2011). We provided an analysis of our model formulation to hypothetical temperature changes. For this we require additional model development, consistent with our enzyme kinetic formulation. Since POC receives plant-derived materials as inputs (McGuire and Treseder 2010), we assumed that the POC pool consists of two substrates (lignin and cellulose/hemicellulose). Each substrate has associated enzymes that convert it into dissolved monomers (DOC). Lignin is decomposed by oxidative enzymes (ligninases) produced by appropriate microbes (fungi), and cellulose/hemicellulose is decomposed with hydrolytic enzymes (cellulases) produced by bacteria and fungi (Wang et al. 2012b). The allocation of EP production to ligninase and cellulase was presumed to be proportional to the corresponding substrate pool size. We investigated the SOC pools changing with time under warming conditions by conducting numerical simulations.

The Arrhenius equation was used to simulate the response of parameter values to changes in temperature (Wang et al. 2012b):

\[ V(T) = V(T_{ref}) \exp \left[ -\frac{E_a}{R} \left( \frac{1}{T} - \frac{1}{T_{ref}} \right) \right] \]  

where \( V(T) \) and \( V(T_{ref}) \) are the parameter values at the temperature \( T \) (K) and the reference temperature \( T_{ref} \) (K), respectively; \( E_a \) is the energy of activation (kJ/mol); and \( R = 8.314 \, J \cdot mol^{-1} \cdot K^{-1} \), is the universal gas constant.

The activation energy (Ea) in the Arrhenius equation for selected parameters is shown in Table 3. The specific reaction rate for lignin degradation had a higher Ea than that of cellulose (Wang et al. 2012b). Ea for the half-saturation constants \( (K_p, K_M, \text{and } K_P) \) was set as 30 kJ/mol, corresponding to a \( Q_{10} \) of 1.5 for temperature ranging 20–30°C (Davidson et al. 2006). The microbial maintenance is also dependent on temperature (van Iersel and Seymour 2002). Elshafei et al. (2009) observed a low Ea, i.e., 4.36 and 5.04 kJ/mol for DOC adsorption in clay and sandy soils, which was consistent with the observations of no apparent effect of temperature on it (Kaiser et al. 2001, Mehdi et al. 2009). As shown in Table 3, Ea for adsorption is smaller than that for desorption (Conant et al. 2011). The temperature-modification of carbon use efficiency (CUE, denoted by \( E_C \) in equations) is described by a linear function:

\[ E_C(T) = E_C(T_{ref}) - k_{EC}(T - T_{ref}) \]  

where \( 0 < E_C(T) < 1 \) in this study and the slope \( k_{EC} \) was set to 0.012°C⁻¹ (Devevre and Horwath 2000).

The baseline soil temperature and pH value were set as 12°C and 6, respectively. The baseline temperature of 12°C is close to the mean annual temperature of 11.6°C for the United States (NOAA 2011). The baseline pH of 6 is the mean soil pH value calculated from literature data (see Table 4).

We simulated the responses of C pool sizes to a temperature increase of 2°C against the control treatment (12°C) by sampling the parameters from their respective distributions/ranges. Only those parameter sets that could result in a feasible steady-state system were used for further analysis. The steady-state C pool sizes were then adopted as initial values for scenario analysis over a 100-yr period. The values of parameters shown in Table 3

Table 4. Summary of soil organic carbon data from the literature (the associated full data are presented in the Supplement).

<table>
<thead>
<tr>
<th>Soil order</th>
<th>n</th>
<th>log₁₀(SOC)</th>
<th>n</th>
<th>log₁₀(DOC)</th>
<th>n</th>
<th>log₁₀(MBC)</th>
<th>n</th>
<th>pH</th>
</tr>
</thead>
<tbody>
<tr>
<td>Allsols</td>
<td>154</td>
<td>1.19 ± 0.30</td>
<td>18</td>
<td>−0.79 ± 0.56</td>
<td>25</td>
<td>−0.33 ± 0.41</td>
<td>141</td>
<td>6.3 ± 0.7</td>
</tr>
<tr>
<td>Aidsols</td>
<td>52</td>
<td>1.77 ± 0.21</td>
<td>34</td>
<td>−0.64 ± 0.30</td>
<td>28</td>
<td>−0.60 ± 0.45</td>
<td>45</td>
<td>5.8 ± 0.9</td>
</tr>
<tr>
<td>Andisols</td>
<td>33</td>
<td>0.92 ± 0.39</td>
<td>4</td>
<td>−0.96 ± 0.26</td>
<td>1</td>
<td>−0.45</td>
<td>21</td>
<td>7.6 ± 0.4</td>
</tr>
<tr>
<td>Entisols</td>
<td>81</td>
<td>0.94 ± 0.54</td>
<td>17</td>
<td>−1.56 ± 0.52</td>
<td>14</td>
<td>−0.44 ± 0.72</td>
<td>61</td>
<td>6.3 ± 1.2</td>
</tr>
<tr>
<td>Gelisols</td>
<td>49</td>
<td>1.77 ± 0.63</td>
<td>21</td>
<td>−0.51 ± 0.42</td>
<td>7</td>
<td>0.58 ± 0.69</td>
<td>28</td>
<td>5.4 ± 1.2</td>
</tr>
<tr>
<td>Histosols</td>
<td>44</td>
<td>2.38 ± 0.23</td>
<td>5</td>
<td>0.01 ± 0.35</td>
<td>7</td>
<td>0.23 ± 0.24</td>
<td>21</td>
<td>5.5 ± 1.2</td>
</tr>
<tr>
<td>Inceptisols</td>
<td>204</td>
<td>1.43 ± 0.48</td>
<td>47</td>
<td>−0.86 ± 0.41</td>
<td>62</td>
<td>−0.12 ± 0.32</td>
<td>169</td>
<td>5.8 ± 1.2</td>
</tr>
<tr>
<td>Mollisols</td>
<td>88</td>
<td>1.33 ± 0.31</td>
<td>9</td>
<td>−0.64 ± 0.44</td>
<td>11</td>
<td>−0.18 ± 0.31</td>
<td>75</td>
<td>7.0 ± 1.0</td>
</tr>
<tr>
<td>Oxisols</td>
<td>24</td>
<td>1.41 ± 0.36</td>
<td>7</td>
<td>−1.19 ± 0.85</td>
<td>19</td>
<td>−0.34 ± 0.49</td>
<td>21</td>
<td>5.6 ± 0.8</td>
</tr>
<tr>
<td>Spodosols</td>
<td>62</td>
<td>1.61 ± 0.53</td>
<td>20</td>
<td>−0.92 ± 0.50</td>
<td>14</td>
<td>−0.08 ± 0.47</td>
<td>56</td>
<td>4.7 ± 0.9</td>
</tr>
<tr>
<td>Ultisols</td>
<td>117</td>
<td>1.15 ± 0.14</td>
<td>14</td>
<td>−1.08 ± 0.41</td>
<td>75</td>
<td>−0.42 ± 0.43</td>
<td>109</td>
<td>5.7 ± 1.0</td>
</tr>
<tr>
<td>Vertisols</td>
<td>18</td>
<td>1.17 ± 0.39</td>
<td>3</td>
<td>−1.56 ± 0.30</td>
<td>12</td>
<td>−0.36 ± 0.24</td>
<td>16</td>
<td>7.3 ± 0.8</td>
</tr>
<tr>
<td>All</td>
<td>916</td>
<td>1.38 ± 0.54</td>
<td>199</td>
<td>−0.85 ± 0.56</td>
<td>275</td>
<td>−0.29 ± 0.48</td>
<td>763</td>
<td>6.0 ± 1.2</td>
</tr>
</tbody>
</table>

Notes: Values are mean ± SD of log-transformed soil organic carbon (SOC), dissolved organic carbon (DOC), or microbial biomass carbon (MBC), measured as mg C/g soil; n is the number of observations. Different superscript letters after means indicate significantly different means according to the Kruskal-Wallis (KW) test at α = 0.05.
were modified by temperature changes. Two scenarios were examined: dynamic CUE, with CUE changing with temperature as described by Eq. 23, and constant CUE, with the same CUE as the control treatment.

We also investigated the temporal evolutions of C pool sizes by conducting model simulations to a hypothetical step-wise temperature change using a single parameter set. The typical parameter values estimated in model parameterization were adopted in this case. The $V_P$ values ($T = 12^\circ C$ and $pH = 6$) for POC-lignin and POC-cellulose were set to 0.96 and 5.02 mg C/mg C$^{-1}$h$^{-1}$, respectively (Wang et al. 2012b). Five scenarios of 1–5°C temperature increase with the parameters showing in Table 3 and CUE changing with temperature were considered. A sixth scenario of 2°C temperature increase with the same CUE (0.47) as the control treatment was also included to compare with the results from the first five scenarios.

RESULTS AND DISCUSSION

Summary of pool sizes from the literature

The KS normality tests on SOC, DOC, and MBC indicated that none of them followed a normal distribution ($P < 1 \times 10^{-10}$). Both log$_{10}$(DOC) and log$_{10}$(MBC) were normally distributed ($P = 0.37$ and 0.71, respectively). Although log$_{10}$(SOC) was not strictly normally distributed ($P = 3 \times 10^{-4}$), we computed the mean and standard deviation (SD) from log$_{10}$(SOC) rather than directly from SOC. Histograms for log-transformed SOC, DOC, and MBC are shown in Fig. 2. Statistics for these data as well as soil pH values classified by soil orders are summarized in Table 4. The soil pH values can be used to modify the decomposition rates through an exponential-quadratic function as described in Wang et al. (2012b). Considering an average soil depth of 0.25 m and bulk density of 1 g/cm$^3$, the back-transformed mean SOC is equivalent to 6 kg C/m$^2$, which is close to the SOC density for cultivated land (7.9 kg C/m$^2$) derived by Post et al. (1982). The enzyme concentration in soils was estimated as $1 \times 10^{-5}$ to $5 \times 10^{-3}$ mg C/g soil (Tabatabai 2003).

Analytical steady-state solutions

Under steady state conditions, the C pools can be analytically determined from Eqs. 1–7 as follows:

\[
P_{eq} = \frac{K_P K_P}{V_P \frac{P_{PEP}}{r_{PEP}} E_C \left( \frac{I_D}{I_P} + 1 \right)} - 1 \approx \frac{V_P \times P_{PEP}}{r_{PEP}} \frac{E_C}{1 - g_D E_C} - 1
\]

\[
M_{eq} = \frac{K_M}{V_M \frac{P_{EM}}{r_{EM}} E_C \left( 1 + I_D \frac{I_D}{I_P} \right) - 1} \approx \frac{V_M \times P_{EM}}{r_{EM}} \frac{E_C}{(1 - g_D E_C)(1 - f_D)} - 1
\]

\[
Q_{eq} = \frac{Q_{max}}{1 + V_D (m_R K_B K_{BA})} = \frac{Q_{max}}{1 + 1/(D_{eq} K_{BA})}
\]

\[
B_{eq} = \frac{I_D + I_P}{(1/E_C - 1) \times m_R}
\]
$I = I_D + I_P$

where $I$ is the DOC uptake rate, $I_D$ is the DOC uptake rate due to enzyme activity, and $I_P$ is the DOC uptake rate due to microbial growth. The parameters $D_{eq}$, $EP_{eq}$, and $EM_{eq}$ are defined as follows:

$D_{eq} = \frac{K_D}{V_D / m_R}$  \hspace{1cm} (28)
$EP_{eq} = B_{eq} \times \frac{m_R p_{EP}}{r_{EP}}$  \hspace{1cm} (29)
$EM_{eq} = B_{eq} \times \frac{m_R p_{EM}}{r_{EM}}$  \hspace{1cm} (30)

where $A = 1 - E$

$C + (1 - p_{EP} - p_{EM}) \times E_C (1 - g_D) (I_D / I_P + 1)$; under the condition of input of DOC/input of POC ($I_D / I_P \ll 1$ and because of $p_{EP} + p_{EM} \ll 1$, $A = 1 - g_D \times E_C$; the subscript eq denotes the steady state solution; and $K_{BA} = K_{ads} / K_{des}$ is the binding affinity (mg C/g soil) as defined in the Langmuir isotherm (Kothawala et al. 2008). The assumption of $I_D / I_P \ll 1$ is based on the consideration that DOC in the mineral soil is derived from decomposed SOC and the DOC input from recent litter is limited (Michalzik et al. 2003, Fröberg et al. 2007).

**Estimation of parameter values**

The parameter values or probability distributions are summarized in Table 5. Some of the parameter values were collected from the literature. Both input rates ($I = I_D + I_P$) and specific maintenance factor ($m_R$) were log-normal distributed (see Fig. 3a and 3b, $P = 0.7$ and $0.2$, respectively). The back-transformed $m_R$ from the log-normal distribution had a mean of $2.8 \times 10^{-4}$ and a 1 SD interval of $(6.3 \times 10^{-5}, 1.3 \times 10^{-3})$. The 1 SD interval for $m_R$ was back-transformed from the 1 SD interval of $log_{10}(m_R)$.

**Table 5. Model parameterization.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Values†</th>
<th>Typical value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I = I_D + I_P$</td>
<td>$log_{10}(I) = -3.8 \pm 0.3$</td>
<td>$1.6 \times 10^{-4}$</td>
<td>Wang et al. (2012b)</td>
</tr>
<tr>
<td>$m_R$</td>
<td>$log_{10}(m_R)$</td>
<td>$-3.6 \pm 0.7$</td>
<td>this study</td>
</tr>
<tr>
<td>$E_C$</td>
<td>0.609–0.012°C</td>
<td>0.47</td>
<td>Devevre and Horwath (2000)</td>
</tr>
<tr>
<td>$f_D, g_D$</td>
<td>0.5 [0.2–0.8]</td>
<td>0.5</td>
<td>Hunt (1977), this study</td>
</tr>
<tr>
<td>$r_{EP}, r_{EM}$</td>
<td>$log_{10}(r_{EP}) = -3.0 \pm 0.5$</td>
<td>$1 \times 10^{-3}$</td>
<td>Allison et al. (2010), this study</td>
</tr>
<tr>
<td>$p_{EP}, p_{EM}$</td>
<td>$log_{10}(p_{EP}) = -2.0 \pm 0.5$</td>
<td>$1 \times 10^{-2}$</td>
<td>this study</td>
</tr>
<tr>
<td>$Q_{max}$</td>
<td>$1.7 \pm 1.1$</td>
<td>1.7</td>
<td>Mayes et al. (2012)</td>
</tr>
<tr>
<td>$K_{BA}$</td>
<td>6 ≤ 5</td>
<td>6</td>
<td>this study</td>
</tr>
<tr>
<td>$K_{ads}$</td>
<td>$1 \times 10^{-3} [10^{-4}–10^{-2}]$</td>
<td>$1 \times 10^{-3}$</td>
<td>this study</td>
</tr>
<tr>
<td>$K_{des}$</td>
<td>$K_{BA} \times K_{des}$</td>
<td>$6 \times 10^{-3}$</td>
<td>this study</td>
</tr>
<tr>
<td>$K_D$</td>
<td>0.26 ± 0.12</td>
<td>0.26</td>
<td>van de Werf and Verstraete (1987)</td>
</tr>
<tr>
<td>$V_D$</td>
<td>$log_{10} (V_D) = -3.3 \pm 0.7$</td>
<td>$5 \times 10^{-4}$</td>
<td>this study</td>
</tr>
<tr>
<td>$V_P$</td>
<td>0.2–33.0</td>
<td>2.5</td>
<td>this study</td>
</tr>
<tr>
<td>$K_P$</td>
<td>$P_{eq}(a_P \times V_P - 1)$, $a_P = 6$ [3–11]</td>
<td>50</td>
<td>this study</td>
</tr>
<tr>
<td>$V_M$</td>
<td>0.05–22.0</td>
<td>1</td>
<td>this study</td>
</tr>
<tr>
<td>$EM_{eq}$</td>
<td>$M_{eq}(a_M \times V_M - 1)$, $a_M = 14$ [4–51]</td>
<td>250</td>
<td>this study</td>
</tr>
</tbody>
</table>

**Notes:** See Table 2 for description of parameters; $f_D$ denotes the model inputs.

† Values shown are means; error is SD, ranges in brackets are lower bound and upper bound.

$D_{eq}$ were assumed to be 0.5 (Hunt 1977). The average C contents from all observations (Table 4) were used as steady-state pool sizes.

From Tabatabai (2003), the estimated enzyme concentration of α-glucosidase and β-glucosidase ranges from $1 \times 10^{-3}$ to $5 \times 10^{-3}$ mg C/g soil, with a mean value of $2 \times 10^{-4}$ mg C/g soil, assuming that it follows a log-normal distribution. Considering that “the actual concentrations of enzyme proteins in soils are undoubtedly much greater than those calculated” (Tabatabai 2003), we adopted an enzyme concentration of $1 \times 10^{-3}$ mg C/g soil, which is an order of magnitude higher than the mean value. Provided the concentration of equilibrium MBC ($B_{eq}$) from Table 4, specific maintenance factor ($m_R$) and enzyme turnover rate ($r_{EP}$) from Table 5, and enzyme concentration ($EP_{eq}$) = $1 \times 10^{-4}$ mg C/g soil, we estimated the fraction of $m_R$ for production of $EP (p_{EP}) \approx 1\%$ based on Eq. 29. We assumed that $p_{EM} \approx p_{EP}$.

Adapting the values for half-saturation constant of uptake of DOC for MBC growth ($K_P$) from Van de Werf and Verstraete (1987) and DOC concentration ($D_{eq}$) from Table 4, we could estimate the maximum specific uptake rate of DOC for growth of MBC ($V_D$) ≥ $2m_R$ by Eq. 28. For agricultural soils, turnover rates of DOC were found to be $2.5–4.2 \times 10^{-3}$ h⁻¹ (Gjettermann et al. 2008), which was within the range derived in this study.

Generally, the SOC substrates were assumed to be under-saturated (Moorhead and Sinsabaugh 2006, Allison et al. 2010), which implies that the half-saturation constants $K_P$ and $K_M$ have the following relation with steady-state DOC and MOC concentrations, respectively, $0.01 < P_{eq}/K_P < 1$ and $0.01 < M_{eq}/K_M < 1$. The lower bound of 0.01 was set for the two ratios ($P_{eq}/K_P$ and $M_{eq}/K_M$) in order to make the M-M kinetics functional. Carbon use efficiency ($E_C$) is negatively dependent on temperature (Devevre and
Horwath 2000), and $E_C = 0.47$ at $T = 12\degree C$. Eqs. 24 and 25 can be rearranged as follows:

$$P_{eq}/K_P = 1/(a_P V_P - 1)$$

(31)

$$M_{eq}/K_M = 1/(a_M V_M - 1)$$

(32)

where $a_P = p_{ep}/r_{ep} \times E_C/(1 - g_D E_C)$ and $a_M = p_{em}/r_{em} \times E_C/(1 - g_D E_C)/(1 - f_D)$.

With the assumption that $p_{ep}/r_{ep} = 10$, and $f_D$ and $g_D$ $\in (0.2, 0.8)$, we obtained that $a_P \in (3, 11)$ and $a_M \in (4, 51)$. From Eqs. 31 and 32, we plotted $P_{eq}/K_P$ against $V_P$ and $M_{eq}/K_M$ against $V_M$ (Fig. 4). Based on the above constraints for $P_{eq}/K_P$ and $M_{eq}/K_M$, we derived $V_P = 0.2$–33 (mean $\approx 2$) and $V_M = 0.05$–22 (mean $\approx 1$) mg C/mg C$^{-1}$ h$^{-1}$. Allison et al. (2010) set $V = 0.42$ mg C/mg C$^{-1}$ h$^{-1}$ at $20\degree C$, which fell into our parameter range. The $V$ values from laboratory experiments with purified ligninases and cellulases had a 1 SD interval of $1 \times 10^3$ to $1 \times 10^4$ (Wang et al. 2012b), which was at least one order of magnitude higher than the $V$ values derived here.

Jastrow (1996) measured the POC and MOC fractions in long-term cultivated soils and found that they were about 20% and 80% of the SOC contents, respectively. Under the condition of $P_{eq} + M_{eq} = 24$ mg C/g soil (Table 4), one could estimate $P_{eq}$ and $M_{eq}$ as 5 and 19 mg C/g soil, respectively. Using the above $P_{eq}$ and $M_{eq}$ and mean $V_P$ and $V_M$, we calculated that $K_P = 50$ and $K_M = 250$ mg C/g soil, respectively. Similarly, if $P_{eq} + M_{eq} = 110$ as used by Allison et al. (2010), one could derive $K_P = 240$ and $K_M = 1100$, whose range contained the half-saturation constant of 500 mg C/cm$^3$ soil in Allison et al. (2010).

According to Mayes et al. (2012), the binding affinity $K_{BA,L}$ (subscript L denotes the value for the liquid or solution condition) was estimated as 0.06 $\pm$ 0.05 (mg C/L)$^{-1}$. In addition, DOC concentration in mineral soil of temperate forest was $D_{eq,L} = 13.8 \pm 12.1$ mg C/L (Michalzik et al. 2001). Table 4 indicated an average DOC concentration of $D_{eq} = 0.14$ mg C/g soil (1 SD interval, 0.04–0.52). We have assumed that the dimensionless quantity ($D_{eq,K_{BA}}$) in Eq. 26 should be equivalent under different unit systems, i.e., $D_{eq,K_{BA}} = D_{eq,L,K_{BA,L}}$, which yielded $K_{BA} = 100K_{BA,L} = 6 + 5$ (mg C/g soil)$^{-1}$.

Since the analytical steady-state solutions only depended on $K_{BA}$, i.e., the ratio of $K_{ads}$ to $K_{des}$, dynamic analysis (numerical simulation) was conducted to determine the values of $K_{ads}$ and $K_{des}$. The initial values for state variables (Table 1) and typical parameter values (Table 5, specifically $K_{des} = 1 \times 10^{-5}$) were adopted to reach a steady state. These steady-state pool sizes were then used as model initialization with $K_{des}$ varying from $1 \times 10^{-5}$ to $1$ mg C/g soil$^{-1}$ h$^{-1}$. Hourly changes of $Q$ and DOC during the first year (8760 h) are shown in Fig. 5. When $K_{des}$ was reduced from $1 \times 10^{-4}$ to $1 \times 10^{-5}$, the changes in $Q$ and DOC were not significant compared with the others (see Fig. 5a and 5b, respectively). As $K_{des} > 0.01$, both DOC and Q departed from the steady state quickly within the first day. Therefore, we estimated $K_{des}$ as $1 \times 10^{-4}$ to $1 \times 10^{-2}$ mg C/g soil$^{-1}$ h$^{-1}$. The desorption rate in Lawrence et al. (2009) was close to our lower bound of $K_{des}$, because the slow pool in their model is analogous to but larger than the $Q$ pool in our model.

Although we summarized the data of SOC, DOC, and MBC classified by soil orders (Table 4), we did not think there is sufficient information to separately parameterize the model with respect to soil orders. Taking the SOC as an example, there were no significant differences among Gelisols, Spodosols, Andisols, and Inceptisols according to the KW test at $a = 0.05$, neither were among Oxisols, Ultisols, Mollisols, Vertisols, and Alfisols. Therefore, we only estimated the parameters for a “mean” soil type. Actually, the parameterization results shown in Table 5 are proposed general parameter ranges/distributions from considering the parameter uncertainty. In particu-
Fig. 4. Relationship between $P_{eq}/K_P$ or $M_{eq}/K_M$ and $V_P$ or $V_M$. $P_{eq}$ and $M_{eq}$ are equilibrium concentrations, $V_P$ and $V_M$ are maximum specific decomposition rates, and $K_P$ and $K_M$ are half-saturation constants for particulate organic carbon (POC, $P$) and mineral-associated organic carbon (MOC, $M$), respectively. Mean, lower, and upper denote mean value and lower and upper bounds, respectively.

Fig. 5. Determination of desorption rate ($K_{des}$) with binding affinity $K_{BA} = 6$ (mg C/g soil) from dynamics of (a) adsorbed phase of DOC ($Q$) and (b) dissolved organic carbon (DOC).
Table 6. Parameter sensitivity analysis.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>D SI</th>
<th>B Order</th>
<th>P SI</th>
<th>M Order</th>
<th>Q SI</th>
<th>EP/EM Order</th>
<th>CO2 SI</th>
</tr>
</thead>
<tbody>
<tr>
<td>mR</td>
<td>0.083</td>
<td>16</td>
<td>0.087</td>
<td>17</td>
<td>0.024</td>
<td>10</td>
<td>0.011</td>
</tr>
<tr>
<td>ρEP</td>
<td>0.025</td>
<td>13</td>
<td>0.019</td>
<td>12</td>
<td>0.083</td>
<td>16</td>
<td>0.057</td>
</tr>
<tr>
<td>E_r</td>
<td>0.019</td>
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<td>0.056</td>
<td>16</td>
<td>0.036</td>
<td>13</td>
<td>0.039</td>
</tr>
<tr>
<td>pEP</td>
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<td>9</td>
<td>0.018</td>
<td>11</td>
<td>0.059</td>
<td>14</td>
<td>0.039</td>
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<td>K_P</td>
<td>0.006</td>
<td>6</td>
<td>0.003</td>
<td>2</td>
<td>0.143</td>
<td>17</td>
<td>0.038</td>
</tr>
<tr>
<td>V_P</td>
<td>0.108</td>
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<td>0.019</td>
<td>8</td>
<td>0.011</td>
</tr>
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<td>K_M</td>
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<td>15</td>
<td>0.006</td>
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<td>η_E</td>
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<td>0.020</td>
<td>13</td>
<td>0.029</td>
<td>12</td>
<td>0.037</td>
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<tr>
<td>V_M</td>
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<td>0.027</td>
<td>14</td>
<td>0.003</td>
<td>2</td>
<td>0.037</td>
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<tr>
<td>Q_{max}</td>
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<td>0.008</td>
<td>9</td>
<td>0.007</td>
<td>6</td>
<td>0.004</td>
</tr>
<tr>
<td>V_P</td>
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<td>8</td>
<td>0.006</td>
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<td>0.077</td>
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<td>Ψ</td>
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<td>0.003</td>
<td>3</td>
<td>0.039</td>
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<tr>
<td>k_D</td>
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<td>0.035</td>
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<tr>
<td>K_{BA}</td>
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<td>0.006</td>
<td>4</td>
<td>0.006</td>
<td>5</td>
<td>0.007</td>
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<td>12</td>
<td>0.007</td>
<td>8</td>
<td>0.007</td>
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<td>0.005</td>
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<td>Ψ_D</td>
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<td>0.025</td>
<td>11</td>
<td>0.005</td>
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<tr>
<td>K_{des}</td>
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<td>0.003</td>
<td>1</td>
<td>0.003</td>
<td>1</td>
<td>0.002</td>
</tr>
</tbody>
</table>

Notes: Response (state) variables are described in Table 1. For sensitivity index (SI), a greater value indicates more sensitive. Order is the ordering of sensitivity by SI, with a greater number indicating more sensitive.

Sensitivity analysis

Based on the parameterization results shown in Table 5, the MOPSA was conducted in terms of the response variables shown in Table 1. Because we did not differentiate the parameters (enzyme production and loss rates) between EP and EM, the time evolutions of the two pools were the same. Therefore, seven response variables (m = 7, see Table 6) were considered in MOPSA. In addition, although we assumed the fractional input rate (f_D = f_D / f_P) ≤ 1, and f_D = g_D = 0.5 in the steady-state analysis, we adopted uniform distributions for f_D (range, 0.05–1) and f_D and g_D (range, 0.2–0.8) in MOPSA. We also assumed log-normal distributions for r_E (−3.0 ± 0.5 [mean ± SD]) and p_E (−2.0 ± 0.5). In summary, 17 parameters (k = 17) including the C input rates were considered in sensitivity analysis, and the results are shown in Table 6. For each response variable, there were two columns quantifying the sensitivity: the first column showing the SI values and the second column indicating the ordering of the sensitivity based on SI. It is evident that the relative importance of parameters depends on the response variable. For example, the most sensitive (important) parameters for the MBC pool (B) were m_R, E_r, K_P, V_M, f_D, and r_E; the most important parameters regarding POC were K_P, r_E, V_P, p_E, E_r, and f_D; and the Q pool was most sensitive to changes in Q_{max}, m_R, V_P, K_{BA}, K_{des}, and f_D. Several sensitivity plots in terms of MBC are shown in Fig. 6 to illustrate the CPD curves for acceptable and unacceptable parameter values.

As shown in Fig. 7, the overall parameter sensitivity indicated that the maintenance factor of microbial biomass (m_R) was rated highest and the desorption rate (K_{des}) rated lowest among the parameters. Using the k-means clustering (Likas and Vlassis 2003), we classified the 17 parameters into five groups (G1–G5) with sensitivity from high to low: G1 (m_R), G2 (r_E, E_r, p_E, K_P, V_P, K_M, and f_D), G3 (V_M and Q_{max}), G4 (V_P, f_D, and Ψ_D), and G5 (K_{BA}, K_D, g_D, and K_{des}). The parameters within each group were considered to have similar sensitivity. The enzyme production and turnover rates (ρ_EP and r_EP) were as important as the CUE (E_r). Therefore, the function of enzymes in catalyzing SOC decomposition is considerable, although the enzyme concentrations are very small compared to the other C pools. As for adsorption/desorption, the maximum sorption capacity (Q_{max}) was more important than K_{BA} and K_{des}. Although K_{BA} and K_{des} fell into the same group, the SI value for K_{BA} was higher than K_{des}. One of the main objectives of a sensitivity analysis is to evaluate the relative significance of each parameter (Choi et al. 1998, Wang and Chen 2012). The typical sensitivity analysis (SA), which investigates how an observable quantity varies with changes in the parameter, also serves this objective. The more sensitive a parameter is, the more important it is. However, the local SA is conducted in terms of single parameter in the neighborhood of a single parameter value (Van Griensven et al. 2006, Wang and Post 2012). The sensitivity index measures the average “distance” or “difference” between the two cumulative curves, not the “difference” between two means. Determining the sensitivity from the perspective of probability distribution rather than from the simple mean value is one of the advantages of MOPSA over the typical SA. Since computing a P value using the mean and standard deviation requires that a variable follows or can be
transformed to a normal distribution, which is not always true for some variables (e.g., $E_C$, $f_D$, $g_D$). Similar to the other global sensitivity analysis methods, MOPSA varies all the parameters simultaneously. The CPDs of acceptable and unacceptable sets for each parameter (e.g., $m_R$ in Fig. 6a) also account for interactions between parameters (Rodrigue-Fernandez et al. 2012), since the acceptable/unacceptable sets are discriminated by the objective function representing the response of a pool to changes in multiple parameters.

**Temperature effect on SOC dynamics**

The soil C pools could reach a feasible steady state with 3291 out of the 10,000 parameter sets sampled from the parameter distributions/ranges. With an increase of 2°C, the 50% confidence intervals (between the first and third quartiles) of the 100-yr change in C pool size (Fig. 8) indicate (1) the pools of POC-cellulose, MOC, and total SOC increased with dynamic CUE but decreased with constant CUE; (2) the total CO$_2$ production slightly changed (-0.05 to 0.20%) under dynamic CUE and increased (0.12 to 0.77%) under constant CUE; (3) both scenarios caused an increase in DOC and decreases in POC-lignin, $Q$, MBC, and ligninase (EPL); and (4) both cellulase (EPC) and EM decreased under dynamic CUE but cellulase increased and EM remained unchanged under constant CUE. The warming (+2°C) effects considering variations in parameters indicate that the sensitivity of CUE to temperature change had significant effects on all soil C pools except DOC and $Q$. By excluding the outliers shown in Fig. 8, one might conclude that the changes in SOC pools (POC-lignin, POC-cellulose, MOC, $Q$) would vary from -8% to 8% under a 2°C increase in temperature.

The typical parameter values in Table 5 were adopted to examine the C pool sizes changing with time. Five scenarios (I–V) of +1 to +5°C were simulated in addition to the baseline run ($T = 12°C$). As aforementioned, CUE and the parameters shown in Table 3 varied with temperature under scenarios I–V. An additional scenario (VI) was conducted with +2°C and constant CUE. The CO$_2$ efflux (mg C·g soil$^{-1}$·h$^{-1}$; Fig. 9a) reached its

![Fig. 6. Examples of cumulative probability distributions of acceptable and unacceptable parameter values by parameter sensitivity analysis; response variable: microbial biomass carbon (MBC). Parameters are (a) specific maintenance factor ($m_R$), (b) carbon use efficiency ($E_C$), and (c, d) maximum specific enzyme activity for (c) mineral-associated organic carbon ($V_M$) and (d) particulate organic carbon ($V_P$).](image-url)
lowest level during the seventh year under scenarios I–V and resulted in slight decreases of total respiration over 50 years. The CO₂ efflux was higher than the control value during the first 10 years under Scenario VI. Regardless of the scenario, the CO₂ efflux returned to the pre-warming (control) level with very small fluctuations after approximately 10 years, which has been observed in field-based studies (Treseder et al. 2011). After 30 years, the CO₂ efflux completely returned to the control value of 0.16 g C g⁻¹ C₀⁻¹ h⁻¹. This efflux is equivalent to a respiration rate of 1400 g C m⁻³ yr⁻¹ (bulk density = 1 g C/cm³) or 350 g C m⁻³ yr⁻¹ (soil depth = 25 cm), which falls into the observed range of 60–1260 g C m⁻³ yr⁻¹ (Raich and Schlesinger 1992).

Scenarios I–V predicted a net decrease during the first six years and then a net increase in the total SOC contents (POC-lignin + POC-cellulose + MOC + Q; Fig. 9b). Compared to the equilibrium state, the total SOC pool increased after 50 years with scenarios I–V. On the contrary, scenario VI resulted in a continuous decrease in SOC during the first 10 years (Fig. 9b) and a total loss of 6% of the equilibrium pool size after 50 years.

The response of POC-lignin (Fig. 9c) was much more complex than the other pools. Scenario I caused a slight net increase but Scenario II–V predicted net losses of lignin. Scenarios I–V predicted a net gain of POC-cellulose (Fig. 9d) and MOC (Fig. 9e) and higher temperature resulted in greater accumulation of C in these two pools. Unlike the other pools, which stabilized after 30 years, the pools of POC-lignin and MOC did not return to new near-equilibrium states until 50 years because of their relatively low decomposition rates. The net increases in POC-cellulose and MOC led to net gains in the total SOC under scenarios I–V. However, scenario VI with constant CUE resulted in a net decrease in the pools of POC-lignin, POC-cellulose, MOC, and Q. The C loss in the Q pool also increased with higher warming temperature (Fig. 9f) under scenarios I–V. Regardless of constant or dynamic CUE with a temperature increase of 2°C, the Q pool became nearly stable with similar C contents after 20 years, although the temporal trends were opposite during the first 20 years. The Q pool decreased under warming conditions because an increase in temperature would increase the rate of desorption relative to adsorption (Conant et al. 2011).

Net increase in DOC was found for each scenario (Fig. 9g). A constant CUE resulted in less DOC uptake and a large increase of DOC in the first few years, and a net increase in DOC overall. In fact, constant CUE produced a net loss over 50 years for the pools of total SOC, POC-lignin, POC-cellulose, MOC, Q, and MBC (see Fig. 9). In contrast, when CUE is allowed to decrease with warming in scenarios I–V, a net loss of DOC was observed for the first few years, followed by a net increase in DOC. Net increase in DOC was observed most likely because desorption was promoted with higher temperature.

Continuous loss of MBC occurred during the first six years under scenarios I–V (Fig. 9h), which was likely the cause of net loss of DOC in the first few years (Fig. 9g). Net loss in MBC increased with higher warming temperature. In addition, dynamic CUE with a small temperature change (+1°C) resulted in more MBC loss than scenario VI with constant CUE. Similar to MBC, net loss of enzyme was found for each enzyme pool under scenarios I–V (Fig. 9i and j; data for EM is not

![Fig. 7. Overall parameter sensitivity quantified by the sensitivity index with regard to all response variables. Parameters are defined in Table 2.](image-url)
shown here). Under scenario VI, however, net increases occurred for all enzyme pools (Fig. 9i and j) during the first 10 years, which corresponded to the increase in MBC (Fig. 9h). The behavior of MBC and enzyme pools was very different for the constant CUE vs. dynamic CUE, which was the most likely cause of the observed different responses in SOC pools. Because dynamic CUE results in lower MBC and enzyme pools, POC-cellulose and MOC tend to accumulate resulting in the overall increase in SOC (Fig. 9b). Constant CUE, in contrast, tends to over-estimate the activities of MBC and enzymes, leading to lower overall SOC. Similar to the constant CUE scenario, however, POC-lignin decreases with dynamic CUE despite observed decreases in ligninase concentration (Fig. 9i). Different behaviors between the POC-lignin and POC-cellulose pools could be interpreted by the changes in individual enzyme pools and a much higher Ea for the specific lignin degradation rate than for cellulose degradation, which leads to a greater increase in the specific enzyme activity for ligninase than for cellulase under warming conditions. All enzyme pools returned to the baseline sizes after 30 years under scenario VI.

Zhou et al. (2012) found that there is no significant difference in the recalcitrant-C pool between warming (+2°C) and the control for a 10-yr experiment on a tallgrass prairie ecosystem. Our study also indicates the first 10 years as a critical period. The pools of POC-lignin and MOC reached the control values after about 10 years under scenarios I–V (Figs. 9c and e). In particular, POC-lignin decreased in the first three years and then recovered back to the baseline, while very small variations in MOC were observed during the first 10 years.

**Figure 8.** Boxplots of simulated warming (+2°C) effects on soil C pool sizes over a 100-yr period. Parameter values were sampled from their respective distributions/ranges in Table 5. Dynamic CUE means the carbon use efficiency (CUE) varies with temperature. Const CUE denotes that CUE remains the same as the control treatment (12°C). Soil C pools are POCL, particulate organic carbon-lignin; POCC, particulate organic carbon-cellulose; MOC, mineral-associated organic carbon; Q, adsorbed phase of DOC (dissolved organic carbon); SOC, POCL + POCC + MOC + Q; CO₂, total CO₂ production; MBC, microbial biomass carbon; EPL, EPC, and EM, enzymes for POCL, POCC, and MOC, respectively. The bottom and top of the box denote the 25th and 75th percentile (the lower and upper quartiles), respectively. The band near the middle of the box is the 50th percentile (the median). The ends of the whiskers represent the lowest datum within 1.5 IQR (interquartile range) of the lower quartile, and the highest datum within 1.5 IQR of the upper quartile. The data beyond the two ends of the whiskers might be considered outliers.
Although the maximum specific enzyme activities increased under scenario I–V, the decreased MBC led to decreases in enzyme production after several years and then provided negative feedback to decomposition rates. Take scenario II as an example, the concentrations of ligninase and cellulase were reduced by 21% and 14%, respectively, at around the seventh year, compared to the baseline concentrations (see Figs. 9i and j). Although
the maximum specific enzyme activities of ligninase and cellulase were increased by 17% and 11% due to a temperature increase of 2°C, the maximum enzyme activities (maximum specific enzyme activity multiplied by enzyme concentration) were still reduced by 8% and 4% for ligninase and cellulase, respectively, because of the reductions in enzyme concentration. The enzyme activities were also lower under warming than the control from the seventh to the 11th year, which led to accumulation of C in both POC pools under warming conditions in those years. Thus it is understandable that Zhou et al. (2012) observed that the activity of phenol oxidase remained constant and the activity of peroxidase was significantly lower under warming than the control after 10 years. However, during the first year, the activities of ligninase and cellulase were higher under warming than the control, since both maximum specific enzyme activities and enzyme concentrations were higher. Therefore, the positive response of maximum specific enzyme activity combining positive or negative feedback of enzyme concentration to warming could finally result in increased, unchanged, or reduced enzyme activities, mainly depending on the changing magnitudes of specific enzyme activity and enzyme concentration.

**CONCLUSION**

We developed an enzyme-mediated SOC decomposition model with physically measurable pools. Based on the analytical steady-state and dynamic analyses combined with literature estimates, we estimated feasible ranges/distributions for model parameters, such as the maximum specific reaction rates and half-saturation constants for the decompositions of POC and MOC and the uptake of DOC by MBC, the specific maintenance factor and the adsorption and desorption coefficients. The scenario analysis of responses of SOC dynamics to warming indicated that the decreased MBC under warming conditions might lead to decreases in enzyme production and provide negative feedback to decomposition rates. Although the maximum specific enzyme activities increased with increasing temperature, the overall decomposition rates were reduced and the total SOC yielded net accumulation of C over 50–100 yr with regard to warming and dynamic CUE, while a constant CUE might result in a net SOC loss. Our model simulation indicated that SOC losses under warming conditions could occur in the first few years, and subsequently recover because of reductions in decomposition resulting from reductions in microbial biomass and associated enzyme production.

Multiple SOC pools (POC-lignin, POC-cellulose, MOC, and Q) in the MEND model elucidate different responses of various pools to temperature changes and the contributions of various pools to the overall SOC dynamics, which is more informative than the model with a single SOC pool (e.g., Allison et al. 2010). Different behaviors between the POC-lignin and POC-cellulose pools could be interpreted by the changes in individual enzyme pools and a much higher Ea for the specific lignin degradation rate than for cellulose degradation. The dynamics of different SOC pools reflected the catalytic functions of specific enzymes targeting specific substrates and the interactions between microbes, enzymes, and SOC.

The feasible parameter values and the MOPSA method developed in this study can be used as useful tools to parameterize the decomposition models incorporating microbial-enzyme kinetics. Our current model simplifies the descriptions of enzyme dynamics and the relationships to microbial dynamics. Further steps to incorporate enzyme patterns and responses to substrate chemistry and microbial stoichiometry (Sinsabaugh et al. 2008) into mathematical models will be required for a complete process description.

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**LITERATURE CITED**


Supplemental Material

Supplement

Full data for soil organic carbon (SOC), dissolved organic carbon (DOC), and microbial biomass carbon (MBC) collected from the literature (Ecological Archives A023-015-S1).